

# Effect of wear on the dynamics of structures with friction contacts

33° Cycle Annual PPT (2017-2020)

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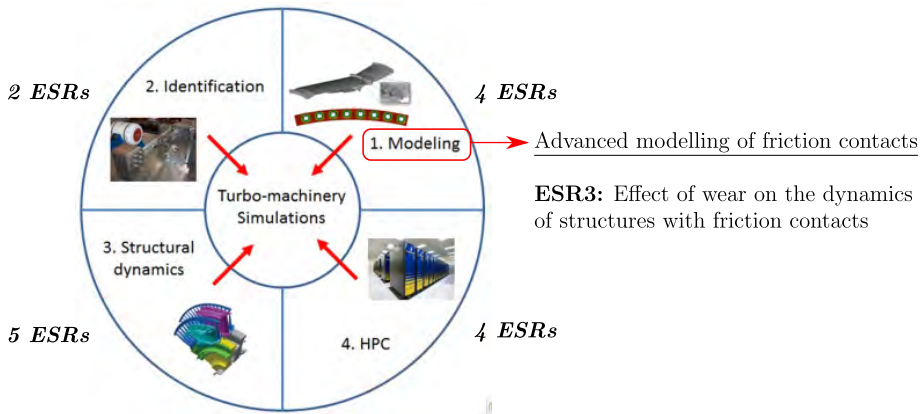
17-12-2020 — PoliTo

# Outline

- 1 Motivation
- 2 Theory
- 3 Test cases
  - Cantilever Beam
  - Bladed Disk
- 4 New Test Rig
- 5 Conclusion
- 6 Appendix
  - Industrial Test Case
  - HPC

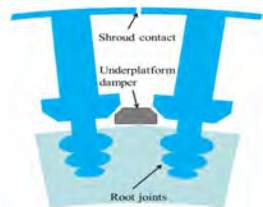
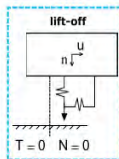
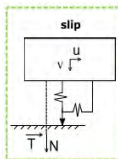
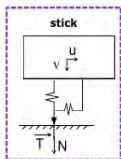
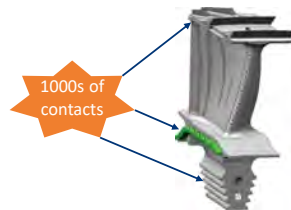


# EXPERTISE - Horizon 2020 ETN

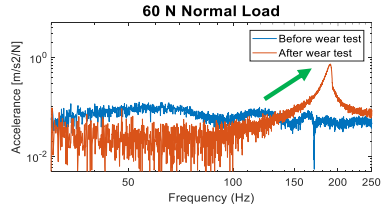
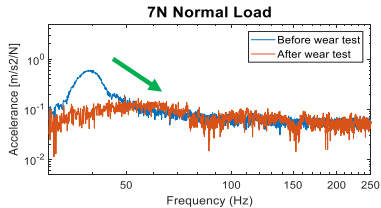
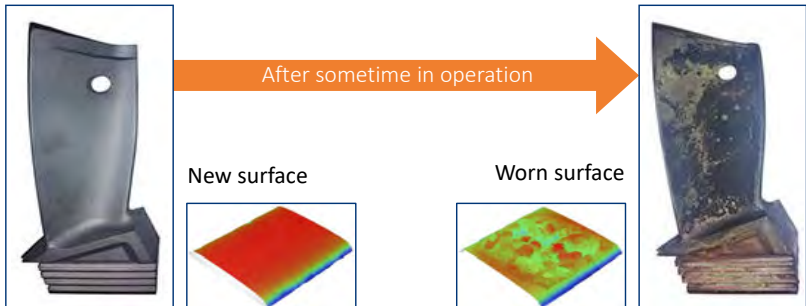


The ultimate research objective of EXPERTISE is to develop advanced tools for the dynamics analysis of large-scale models of turbine components to pave the way towards the virtual testing of the entire machine.  
[Grant No. 721865]





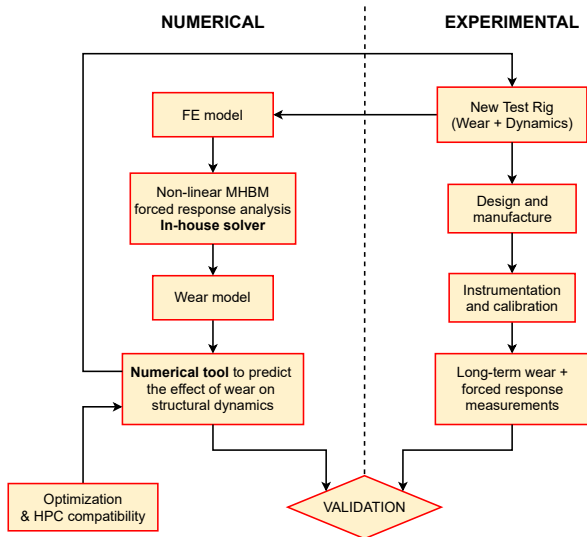
- <sup>1</sup>Md Afzal Licentiate thesis. KTH 2015. <https://pdfs.semanticscholar.org/a8c9/accd7a4e6de20cc0e7108f9afc14697fe564.pdf>
- <sup>2</sup>Gastaldi, C. PhD Course: Models and methods for the dynamics of mechanical components with contact interfaces. Politecnico di Torino. 2016.



# Objectives

- To develop and validate models to predict the effect of wear on the contact surfaces and their ability to dissipate energy by damping thereby affecting dynamics of structures with friction contacts
- The validated models to be embedded in non-linear solvers for forced response of turbine components

# Expected Outcome



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# Formulation

## Equation of motion: Time Domain

$$M\ddot{x}(t) + C\dot{x}(t) + Kx(t) = F(t) + F_{nl}(x, \dot{x}, t)$$

## Frequency Domain

$$Q(t) = \Re \left( \sum_{h=0}^H \hat{Q}^{(h)} e^{ih\omega t} \right) \mid \{x, F, F_{nl}\} \in Q$$

## Harmonic Balance Method (HBM)

$$D^{(h)} \hat{x}^{(h)} = \hat{F}^{(h)} + \hat{F}_{nl}^{(h)} \text{ with } h = 0..H$$

$$\text{where } D^{(h)} = ((-h\omega)^2 M + ih\omega C + K)$$

## Residual equation

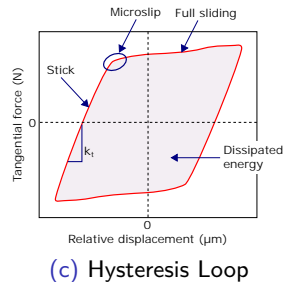
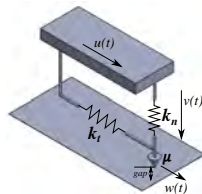
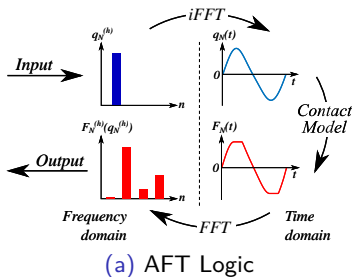
$$RES^{(h)} = D^{(h)} \hat{x}^{(h)} - \hat{F}^{(h)} - \hat{F}_{nl}^{(h)}$$

## Using coupled static/dynamic Harmonic Balance Method<sup>1</sup>

<sup>1</sup> Firrone, C.M, Zucca, S, Gola, M.M, "The effect of underplatform dampers on the forced response of bladed disks by a coupled static/dynamic harmonic balance method", *International Journal of Non-Linear Mechanics*, 46(2), pp. 363-375, 2011.   

# Alternating Frequency Time (AFT) Logic

- Friction contact non-linearity
- 2-D Jenkins element with variable normal load
- Contact states: Stick, Slip, Lift-off



# Modelling wear

- Using wear energy approach<sup>2</sup>

$$v_w = \frac{Z}{A} \alpha E$$

where,

$v_w$  wear depth

$Z$  number of cycles

$A$  associated contact area of the node pair

$\alpha$  wear energy coefficient

$E$  energy dissipated

$v_w$  is introduced to the 0<sup>th</sup> order coefficient of the relative displacement in the normal direction

$$v(t) = \sum_{h=0}^H \hat{v}^{(h)} e^{ih\omega t} - v_w^{(0)}$$

<sup>2</sup>M. Z. Huq and J. P. Celis, "Expressing wear rate in sliding contacts based on dissipated energy," *Wear*, 2002.

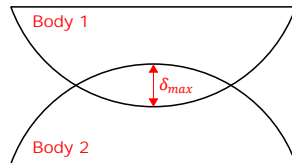


# Modelling wear – contd.

## • Adaptive wear logic

Nodal wear depth after 1 vibration cycle:  $\Delta h_{ij}$

$$Z = \text{floor} \left( \frac{v_{W,max}}{\max(\Delta h_{ij})} \right) \gg 1$$



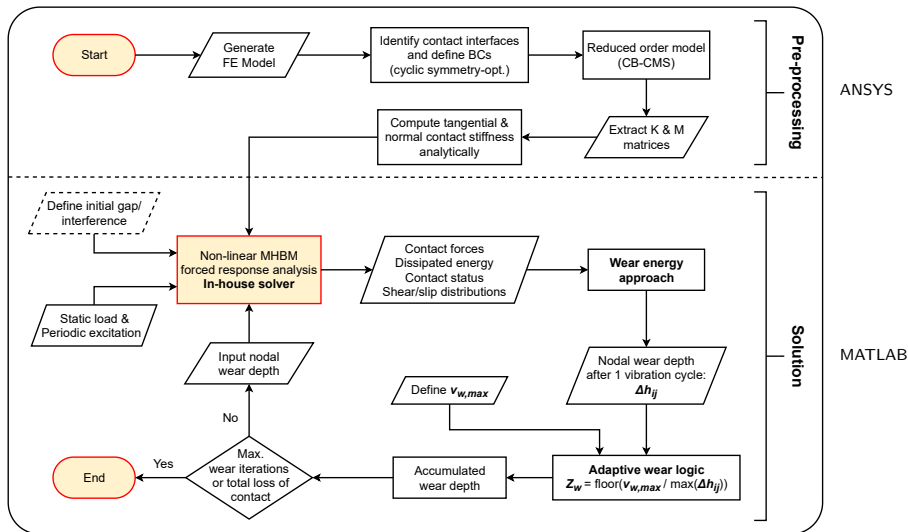
$v_{W,max}$  is a user defined parameter. It can be defined by:

- the maximum wear depth allowed for each wear iteration
- the percentage of the maximum static deflection ( $\delta_{max}$ ) for the given static loads acting at the contact
- the maximum tolerable error percentage in wear depth

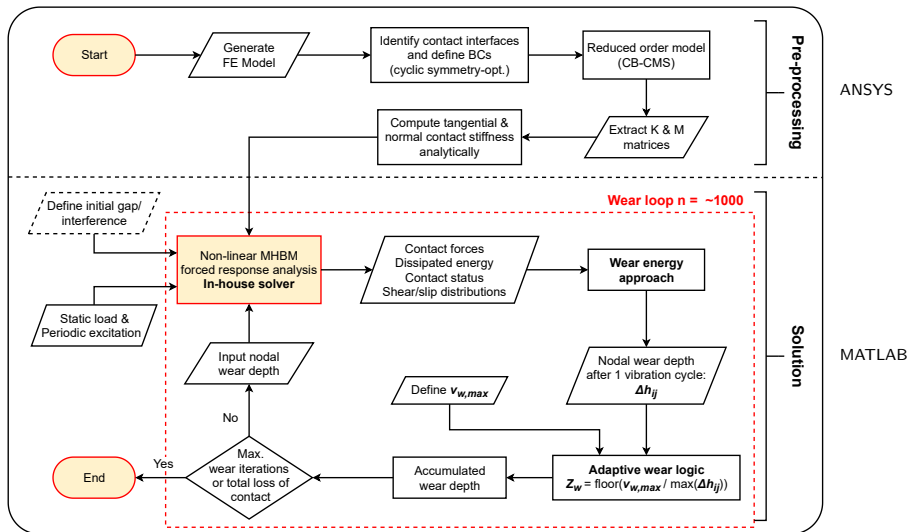
<sup>3</sup> J. Armand, L. Pesaresi, L. Salles, and C. W. Schwingshackl, "A Multiscale Approach for Nonlinear Dynamic Response Predictions with Fretting Wear," *J. Eng. Gas Turbines Power*, vol. 139, no. 2, pp. 1–7, 2017.

<sup>4</sup> Tamatam, L. R., Botto, D. and Zucca, S. (2019) 'Effect of wear on the dynamics of structures with contact interfaces by a coupled static/dynamic multi-harmonic balance method', in *First International Nonlinear Dynamics Conference. Book of abstracts*, pp. 129–130

# Solution flowchart



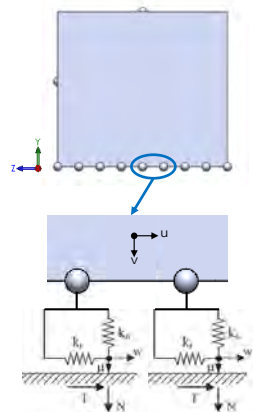
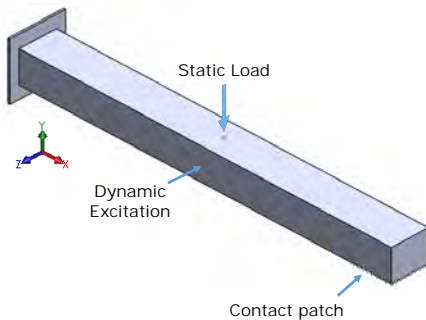
# Solution flowchart



# Outline

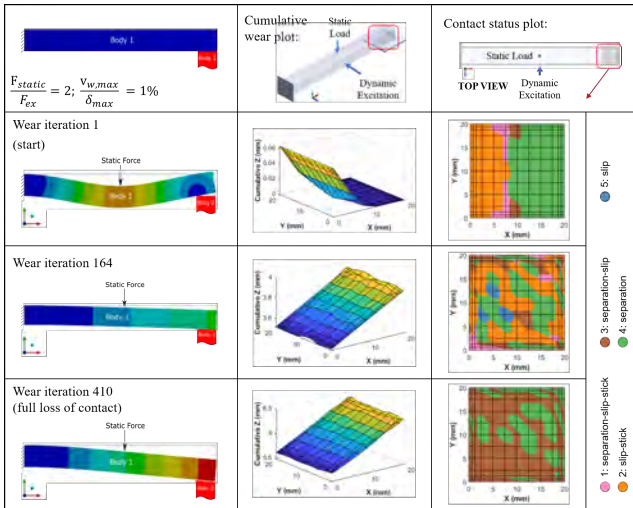
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# Test Case: Cantilever beam



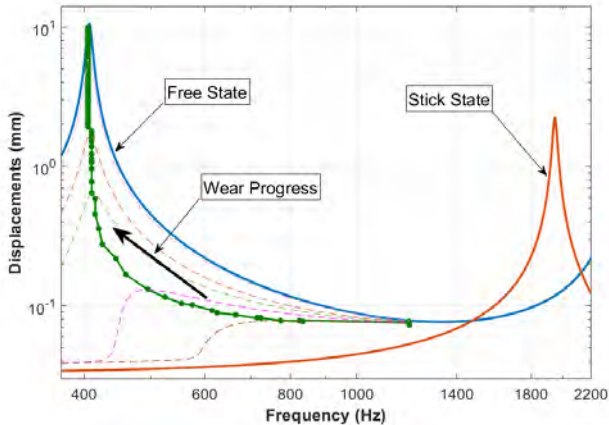
# Effect of wear

- Cumulative wear depth and contact status at different wear iterations:

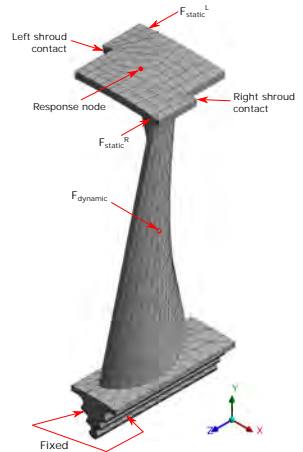
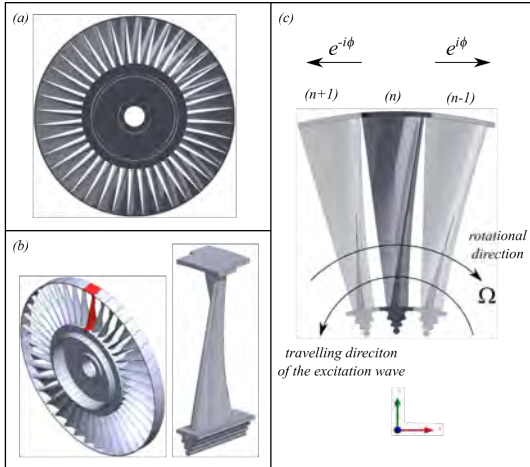


# Effect of wear

- Response plot with backbone of non-linear forced response:



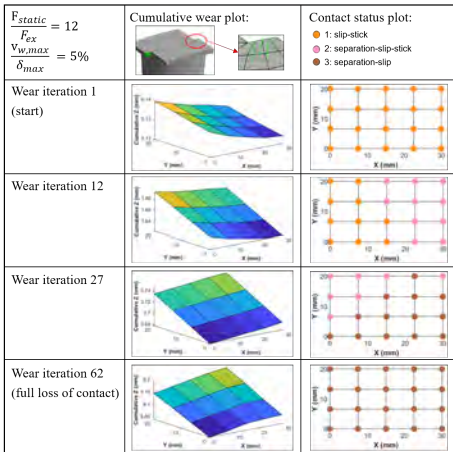
# Shrouded bladed disk



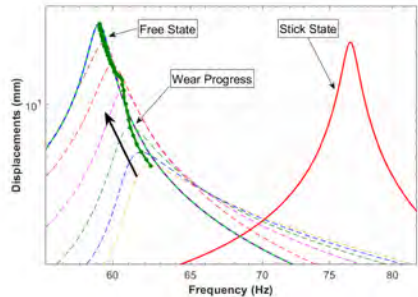


# Effect of wear

## Contact interface evolution



## Dynamic response



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# New Test Rig

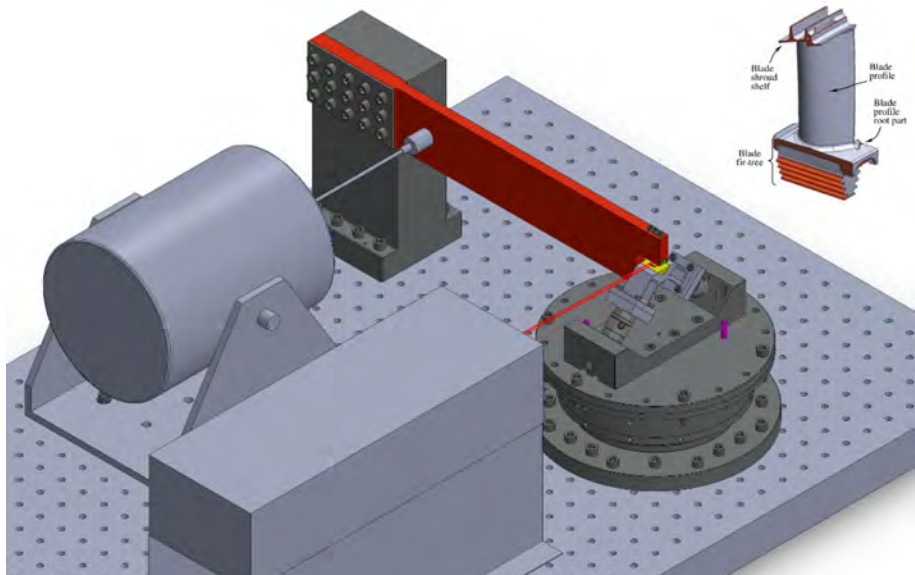
## Goal:

- To design a new Test Rig to investigate the effect of wear at the friction contact on the long-term forced response of the structure

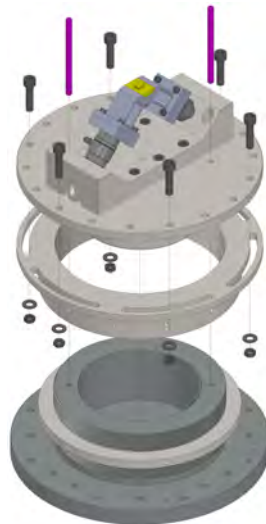
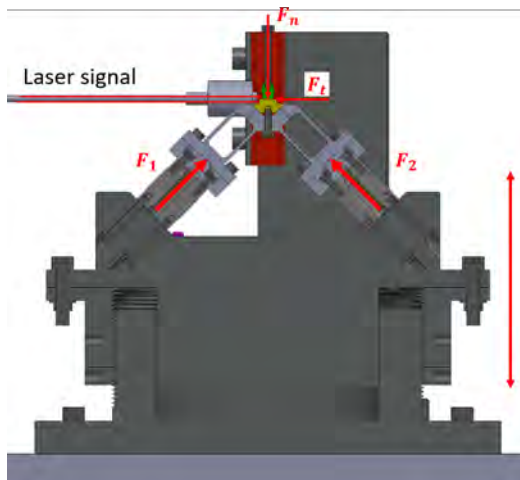
## Requirements:

- Clean system FRFs to be able to quantify the effect of wear
- In-situ dynamic response measurement at various wear intervals
- Mechanism to apply static contact pre-load
- Ability to simulate varying contact pre-load with progressing wear
- Ability to study contact surface evolution

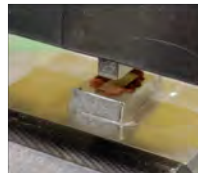
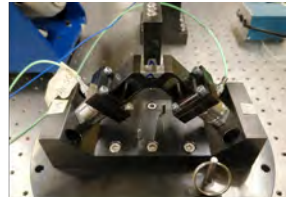
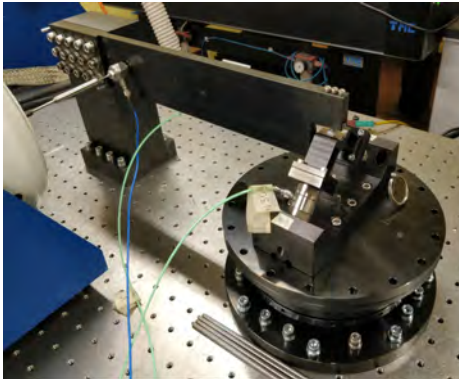
# Iso view



# Contact loading mechanism - screw lift system

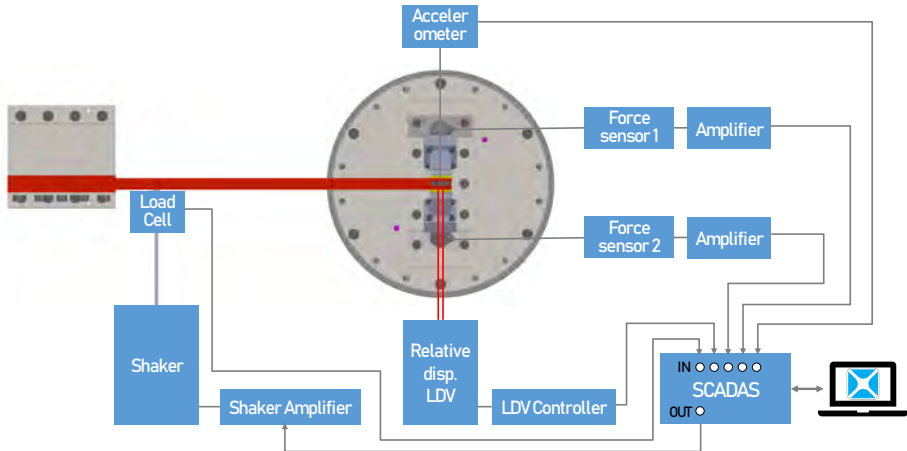


# Test rig pictures



<sup>5</sup> L-separator adapted from: Botto, Daniele Umer, Muhammad. (2018). A novel test rig to investigate under-platform damper dynamics. Mechanical Systems and Signal Processing. 100. 344-359. 10.1016/j.ymssp.2017.07.046.

# Instrumentation



# Measured quantities

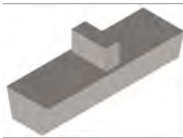
## For wear:

- Relative displacement at the contact using Laser
- Tangential contact force [ $F_t = F_1 \cdot \cos(45^\circ) - F_2 \cdot \cos(45^\circ)$ ]
- Normal contact force [ $F_n = F_1 \cdot \cos(45^\circ) + F_2 \cdot \cos(45^\circ)$ ]
- Excitation force via Load Cell at the shaker-beam interface

## For FRF:

- Accelerometer

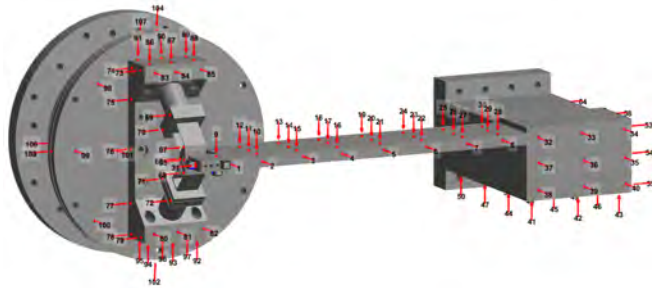
## Consumables: Body 1 & Body 2





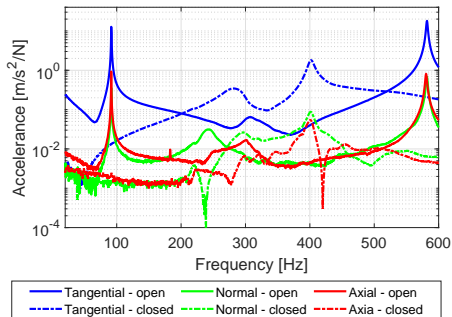
# Roving Impact Hammer setup

- 107 impact points to visualize experimental mode shapes
- Performed on open and closed contact

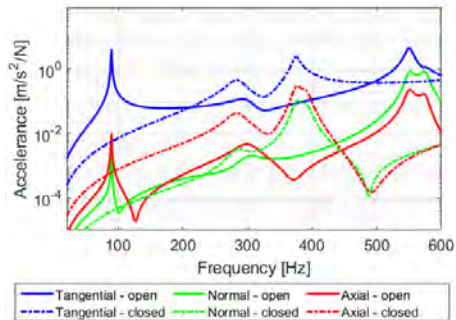


# System FRFs

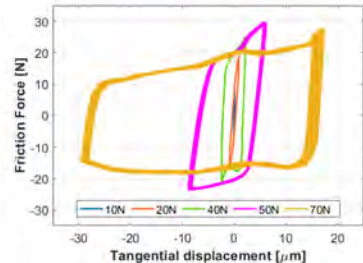
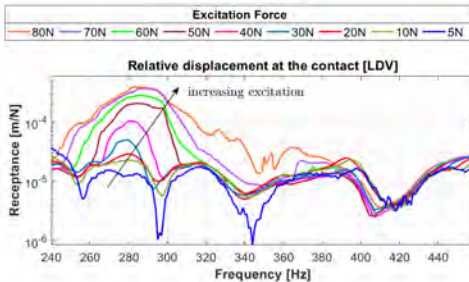
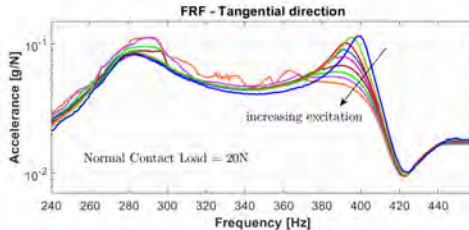
## Experimental



## Numerical with tuned joints

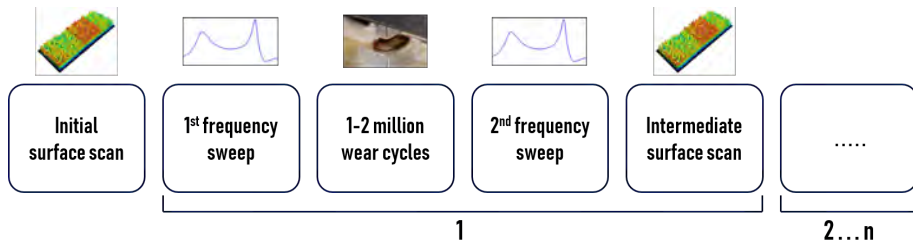


# Effect of excitation on FRFs and resulting hysteresis loops



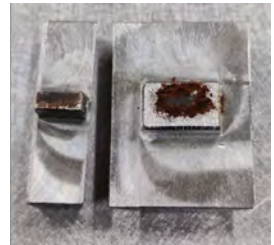
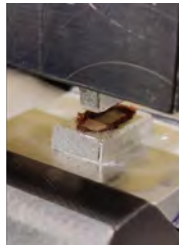
# Test plan

Forced response + wear:

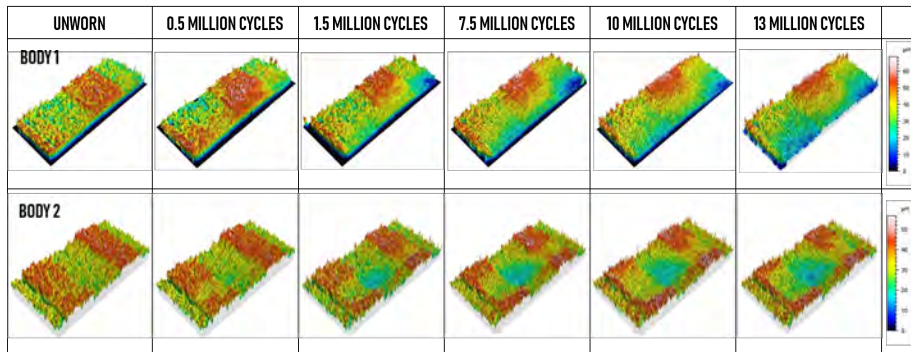


# Worn specimens: Close-up

- Nominal contact area =  $2 \times 5 \text{ mm} = 10 \text{ mm}^2$
- Static pre-load = 28 N
- Excitation force = 70 N @ 280 Hz
- 13 million fretting wear cycles



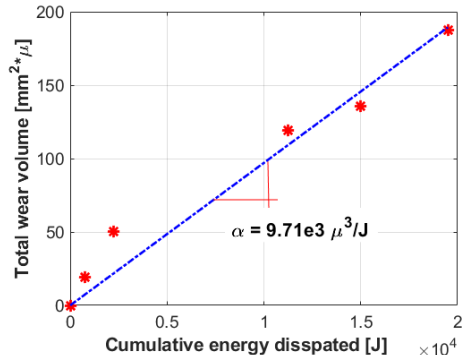
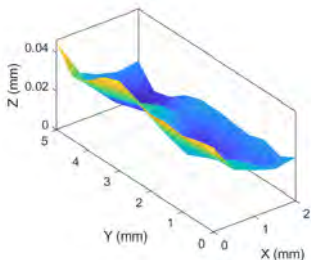
# Specimen surface scans



# Wear volume vs. Energy dissipated

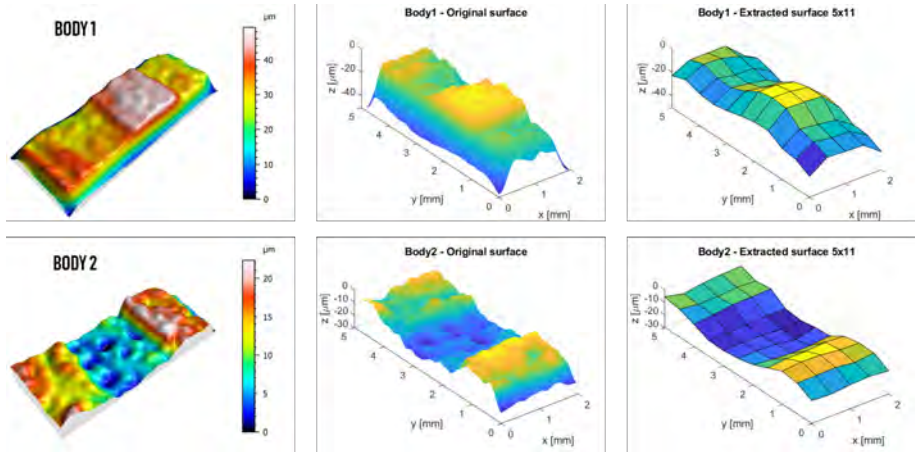
Wear energy co-efficient

Cumulative wear profile



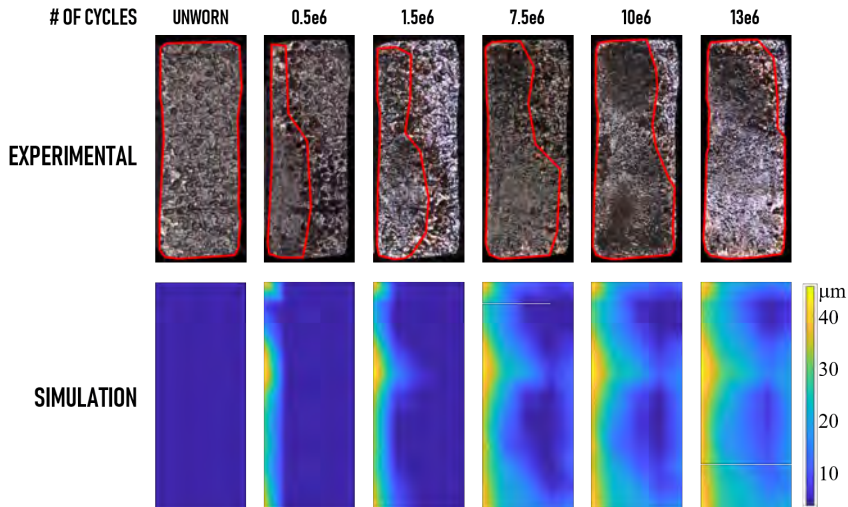
# Extracting real surface profile for HBM Simulation

- Extract waviness and down-sample to match mesh grid (5x11 nodes)

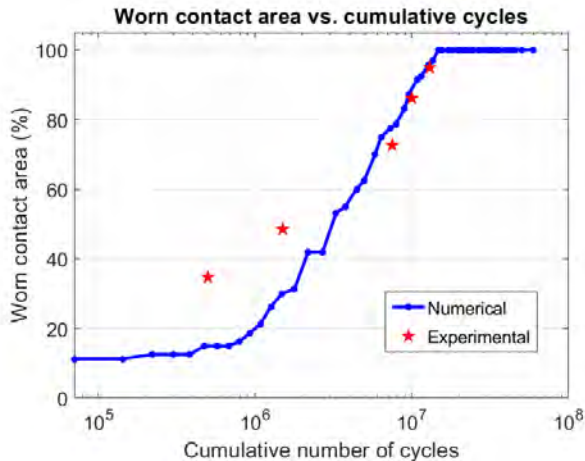




# Contact interface evolution



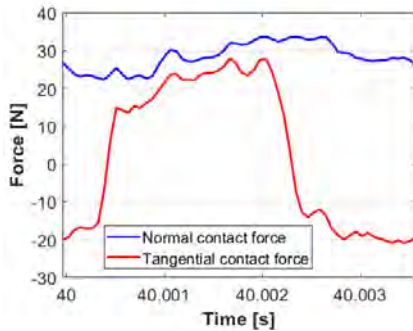
# Establishing real contact area



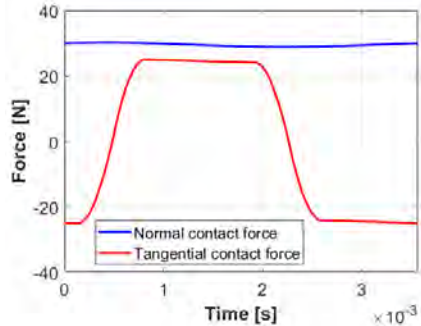
# Contact forces

- Snapshot of contact forces in one vibration cycle

## Experimental

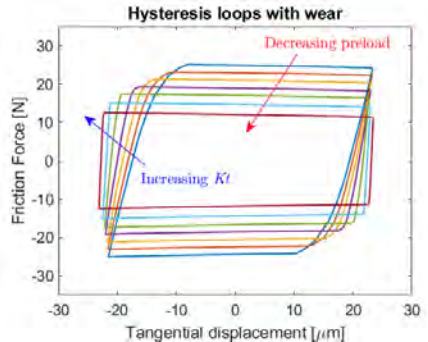
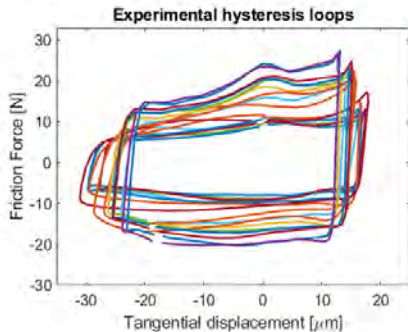


## Numerical

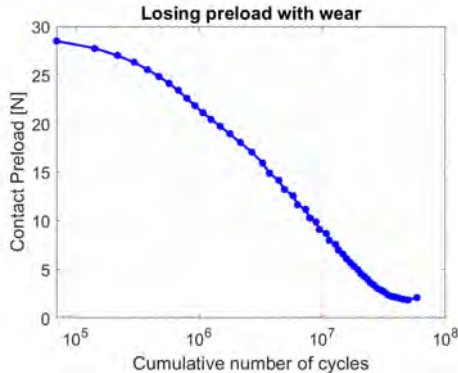


# Evolution of Hysteresis loops

# Experimental vs. Numerical Hysteresis loops



# Effect of wear on static pre-load

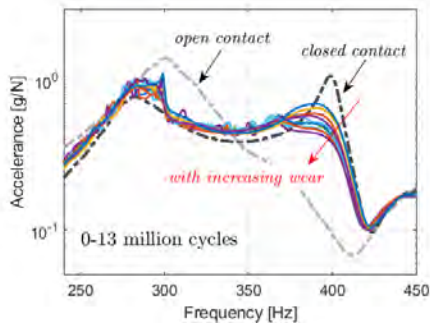


For the given geometry, material and loading conditions, 50 million cycles is not large enough life for a turbomachinery component.

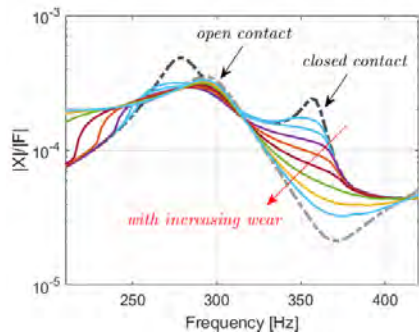
An engine operating continuously at 3000 rpm excited at 1 engine order takes only 11.5 days to full lose the contact!

# Effect of wear on the dynamic response

## Experimental



## Numerical



# Test rig: Conclusions

- Successful setup of the test rig, instrumentation, calibration and initial run
- Studied the evolution of contact interface due to wear and the effect on FRFs
- Extracted the contact parameters through hysteresis loops
- Studied the changing static pre-load phenomenon due to wear
- **First of its kind dedicated experimental test rig to study wear and the effect on dynamics with friction contact and changing pre-load**

## Numerical simulation:

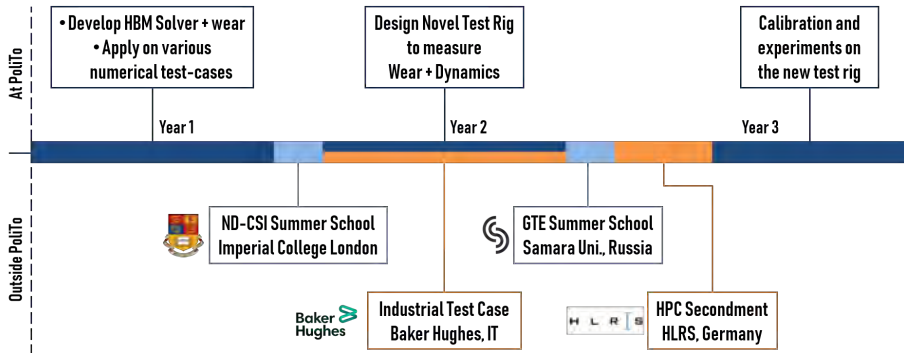
- Created an FE model of the test rig mimicking real boundary conditions
- Successful run of HBM and performed the effect of wear simulation
- Model needs fine tuning to match the natural frequencies accurately
- Simulated the effect of changing pre-load and the effect on wear evolution and FRFs



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# Summary



# Acknowledgements



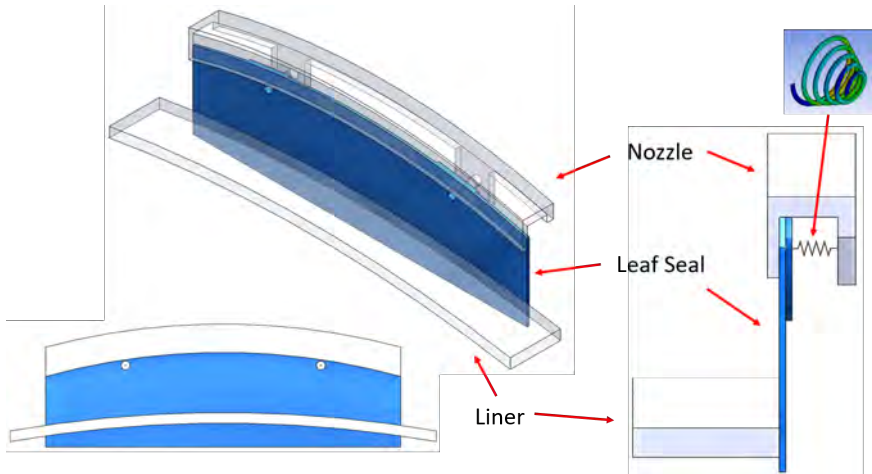
This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 721865.

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# Gas Turbine Combustor Leaf Seal Overview

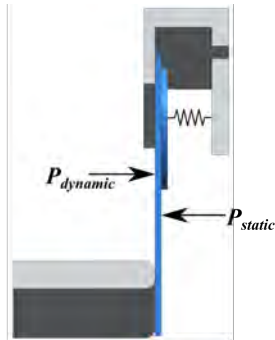
Industrial collaboration with Baker Hughes, Florence, Italy



# Kinematic & operating envelope



**Outward position**



**Vertical position**

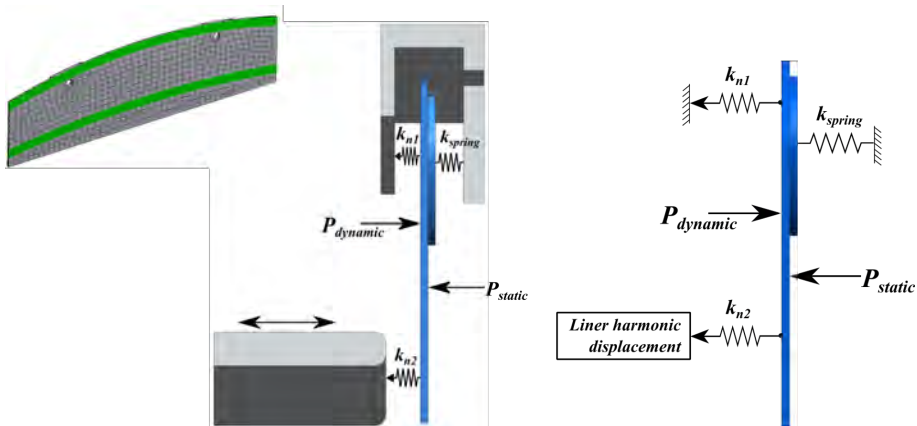


**Inward position**



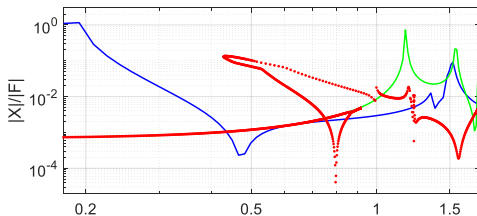
# Schematic

- Schematic for dynamic analysis:

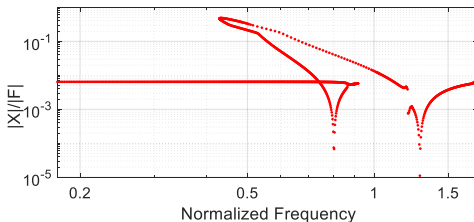


# Dynamic results

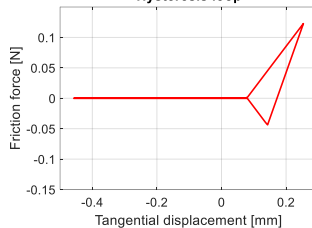
1<sup>st</sup> Harmonic



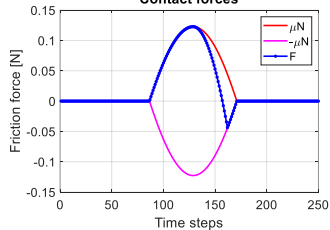
0<sup>th</sup> Harmonic



Hysteresis loop



Contact forces





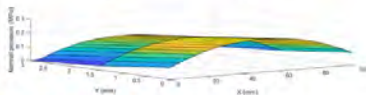
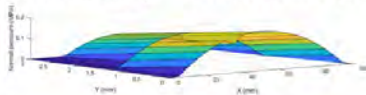
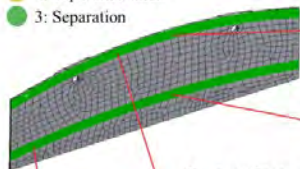
# Contact kinematics

Contact status:

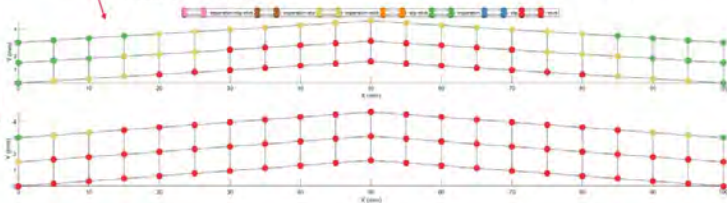
- 1: Stick
- 2: Separation-stick
- 3: Separation

$F_{static} = -90N$ ;  $F_{dynamic} = 30N$ ; @ frequency = 199.5459 Hz; liner disp = [3 0]

Contact Pressure plots:



Contact Status plots:



# HPC Secondment overview

Location: HLRS, Stuttgart, Germany

## Goal:

- To study the feasibility of parallelization and HPC compatibility of the in-house developed HBM solver

## Outcome:

- Learnt the basics of High Performance Computing to understand the hardware and software requirements
- Analyzed the bottlenecks relating to my code in terms of efficiency and MATLAB
- Parametric study on the size of non-linear problem, effect of harmonics and various input parameter space
- Achieved 80% reduction in run-time by re-writing parts of code and optimizing the instruction set compared to Supercomputer with personal computer
- High-level overview study of available external packages, programming languages and pros and cons of each routine specific to the non-linear dynamics domain

# HPC – Bird's eye view

